Surveying Through Solid Walls

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Abstract

A good metrology system in the automated environment must (1) measure the three dimensional position and attitude of any component to a reasonable degree of accuracy; (2) acquire these data fairly rapidly; and (3) be capable of making reliable measurements anywhere on site. A significant limitation for existing surveying systems (including GPS and laser based technologies) is the requirement for direct line-of-sight between the reference and roving surveying elements. Construction sites, as a rule, are highly unstructured environments and clutter is the norm. Recent fundamental research has been undertaken at NIST to develop a real-time Non-Line-of-Sight measurement system capable of tracking to 10 mm accuracy despite the presence of walls, ceilings, floors, and other obstructions. The new system determines the distance from a series of reference transmitters which broadcast pulse-synthesized baseband electromagnetic signals. Digital signal processing techniques are used to recover the time of flight (and hence distance) and to compensate for errors introduced as a result of material penetration and retransmission of the signal. Results of the most recent series of NIST laboratory investigations leading towards a practical construction metrology system are discussed.

1: Introduction

The NIST program in Construction Automation seeks to develop, integrate, and implement new technologies which will permit generalized automation at the construction job site. Research is presently focused on methods and standards for closing the information loop from the job site to a central dynamic, evolving project database, and returning information from that database in an on-demand, real-time format to a wide variety of users at the construction site. Current research includes the development of a real-time, nonline-of-sight surveying system that can "see through walls;" the development of the National Construction Automation Test Bed for testing various automation mechanisms, standards, and software; the development of kinematic representation standards for construction machinery and components; and the development of standards for wireless data telemetry packets for transmission of information from the active job site to a high bandwidth trunk line which links the various project participants.

Each of the above research areas leverage upon the rapid advance of information technology and infrastructure that has occurred during the last decade and is still continuing. The emergence of high speed computer communication networks (the "information superhighway") and real-time, immersive, computer graphics (virtual reality) technologies presage the imminent ability to manage remote construction sites from central offices; to automate certain portions of the tasks performed by common construction machines; and to provide information on the state of such machines to operators (on-site or remote) that would greatly enhance their productivity. Limited demonstrations of this type of technology, largely relating to the control of robotic spacecraft and, more pertinently, to the tele-operation of simple machines for the handling of nuclear waste, have been conducted.

In order to achieve acceptance in the construction industry, a standard means of rapidly interfacing any piece of machinery to a construction-site database must be developed. The development of this standard is highly unlikely to be addressed by the construction industry itself, where corporate research budgets are small in the United States. Nor will it be developed by equipment manufacturers who, left to their own devices, tend to develop closed, proprietary systems which by their very nature inhibit the free exchange of data with other systems that might be operational at a In this respect, NIST has been construction site. uniquely positioned, as a neutral entity, to establish the framework for the integration of construction machinery into emerging global database standards. The underpinning to the above technology is the ability to know the real-time position of any piece of equipment and component on the construction site. Present sur-

veying tools suffer from many shortcomings in this regard, the most important of which is that they must operate under line-of-sight conditions. The development of a non-line-of-sight surveying system, which can in effect "see through walls", represents the pinnacle of construction site metrology and has guided the focus of NIST research in Non-Line-of-Sight (NLS) metrology.

Tests conducted at NIST from 1994 through 1997 proved the potential of NLS technology to meet the above objectives [1, 2, 3]. If the technology can be brought to practical implementation the implications are Briefly summarized, the technology profound. involves the use of ultra-wide bandwidth spread spectrum radio signals which are beamed through nonmetallic construction materials as a series of sequential, discrete frequencies. The same approach applies equally well to an impulse baseband transmission. A timedomain response is reconstructed from the frequency power spectrum and the time of flight from transmitter to receiver is calculated by comparing the measured response to a free-space calibration between two or more known points. Problems arise, however, due to non-linear propagation velocities when penetrating solid media. This leads to a delayed arrival of the straight-line (true distance) transmission pulse, thereby producing error in the calculated range.

Other errors arise from scattering (dispersion) of the beam, refraction, and multi-path reflections as well as instrumental error. However, it was demonstrated, by means of qualitative tests in 1994 [1] and by extensive quantitative tests in 1996 [2], that most common construction materials behave as non-conductors and can therefore be successfully penetrated for substantial distances, thereby allowing range measurement. To be more emphatic, unless the building is constructed with seamless metal walls distance measurements are feasible (see [1] for further details).

1.1: Error Compensation

Although proof-of-concept data obtained in 1995 was very encouraging, the accuracies obtained were far from those needed to be practical for machine automation purposes. They were, however, sufficient for other applications, such as personnel tracking in unstructured environments.

Typical solid-propagation measurement errors when penetrating a 500 mm thick slab of concrete were on the order of 800 mm. That is, the measured distance was 800 mm longer than the true distance between the transmitter and receiver. This error was not affected by the range between the transmitter and receiver, thus confirming that most of the error was attributed to the slower phase velocity of the signal as it propagated through the concrete. Thus, a clear path was identified by which the phase propagation error could be compensated. Briefly the approach involves:

1) The development of empirically based statistical models of the electromagnetic characteristics for a large class of construction materials at varying frequencies of transmission and

2) A method by which a real-time mathematical model of the construction site (in the form of CAD solid model elements) can be updated with sufficient robustness to reflect the as-built condition of the site and the material specification of the various components.

Given this foundation it is possible to develop a software algorithm which takes into account the site geometry and material properties and predicts the delay in the arrival of the transmitted pulse due to propagation through engineering materials between the transmitter and receiver. In a more sophisticated variant of this approach all of the physical phenomena associated with wave propagation (including scattering, beating, reflection, and diffraction) may be taken into account and the result used to correct the initial measurement. With sufficient local processing power (in the form of a low power CMOS parallel processor array) such compensations could be made in a kinematic sense with update rates in excess of the 10 to 20 Hz commonly associated with real-time machine control.

Work in 1996 and 1997, which forms the basis of this paper, concentrated on defining propagation and error characteristics of spread spectrum signal penetration through construction materials as a function of the type of material (e.g. glass, concrete, wood etc.), frequency bandwidth, power, signal-to-noise ratio (and techniques, both physical and analytical for improving same), and obstacle geometry.

The resulting experimental data -- which encompass behavior across 8 GHz of bandwidth and comprise one of the most complete sets of information concerning electromagnetic (EM) attenuation in construction materials -- form the basis for the development of autocompensation algorithms which will account for propagation delays as the signal passes through different materials. It is the propagation delay component that accounts for most of the range error.

Ongoing research in 1997 is being directed to developing a range-error compensation model based on non-dispersive ray tracing techniques, which heretofore have largely been used for computer graphics rendering. In this work, CAD models of simulated construction sites are being developed and material characteristics, based on the extensive empirical EM material data acquired in 1996, are being attached to various entities in the CAD model. This model will be used to estimate range error in calculated position determined using the NLS system. It will thus allow conclusions to be drawn concerning the accuracy achievable through NLS, and its limitations and possibly will identify avenues for further resolution enhancement. The more complex phenomenon of EM wave propagation in dispersive media will be addressed in 1998.

2.0 Description of the Invention

The NLS measurement system is based on a variation of a an ultra-wideband synthetic aperture radar in which the receiving antenna was not collocated with the transmitting antenna, as is the case for most traditional bi-static radar systems.

In this study the receiving antenna comprised a roving unit that was located on the opposite side of the material target. In this sense, it was "cooperatively" working with the system, receiving the transmitted signal as opposed to the reflected signal. The microwave transmission system was based on a Hewlett-Packard HP8530 network analyzer/microwave receiver combined with an HP 83623A frequency synthesizer, HP 8511A frequency converter, and an HP 85330A multiple channel controller. A 486 PC-based computer network performed radar control functions, while data calibration and data management were handled with a Pentium PC.

The wideband pulse modulators used for hardware gating and the computer software for system control and data processing were custom developed by Flam and Russell, Inc. of Horsham, PA. MIT Lincoln Lab developed the laboratory test system (detailed in Figure 2.1) and cooperated with NIST researchers on all aspects of the laboratory research and subsequent data reduction. The radar was field-portable with the electronics and computational hardware based in a mid-size van. Table 2.1 lists characteristics of this system. The unit is fully polarimetric and operates over two frequency bands (0.5-2 GHz and 2-18 GHz). In order to measure distance through an obstruction (e.g. a concrete wall), two separate antennas are used, as shown in Figures 2.1, 2.2, 2.3 and 2.5. The receiver becomes a "roving" unit whose position is to be determined. For the situation depicted in Figure 2.1 it is important to recognize that it is the time of flight, determined by performing a chirp-Z transform on the in-phase and quadrature components of the transmitted and received frequency spectrum, that is being measured.

The measured time of flight then converts directly to a straight line distance between the transmitter and receiver as follows:

 $x = c \cdot \delta t$ Eq(2.1) x = straight line distance (m) c = speed of light (300,000,000 m/s) $\delta t = \text{ time of flight (s)}$

Equation (2.1) can determine only the straight line distance from the transmitting antenna to the roving antenna. In order to acquire a unique three dimensional position at least three transmitters are required. The position can then be determined based on three dimensional triangulation. In such calculations it is assumed that precision (mm level) surveys will have been made to establish the benchmark positions of the transmitting antennas.

Returning now to the determination of time of flight, the following simplified summary will assist in helping to understand the NLS concept. First, since accuracy is of primary concern in the design of a precision surveying instrument we concentrate on this first. Speed (update rate) of position is also of great importance for those items requiring real-time feedback (e.g.

Table 2.1: RF Transmission System

Frequencies	0.5-2 GHz, 2-18 GHz
Bandwidth	Antenna limited
Waveform	Gated CW
Pulse Width	10 ns to 500 ns
PRF	50 kHz to 5 MHz
Polarization	Fully polarimetric
Output Power	20 dBm
Dynamic Range	80 dB
Noise Floor	-100 dBm
Designed of the second s	





Figure 2.2: Simplified schematic of the transmission system and means for characterizing the transmitted signal.

automated operation of construction machinery). However, as will become evident, speed is primarily controlled by processor speed, which improves every year. Therefore, the approach discussed below, while designed primarily for accuracy, will nonetheless provide the algorithmic basis for real-time processing as local embedded microprocessors become faster.

Traditional imaging radars and scatterometers [4] make use of a swept frequency for the generation of a frequency response spectrum. An alternative, discrete approach [5] was used for the NIST NLS studies. In this approach, the response of the system is obtained at individual continuous wave frequencies. The discrete step size is user-definable, but for the NIST tests, 401 points were used for the 0.5 to 2.0 GHz experiments and 801 points for the 3.0 to 8.0 GHz experiments. This produced a frequency step size of approximately 3.74 MHz and 6.24 MHz, respectively. Thus, for the 0.5 to 2.0 GHz case, the frequency response spectra was discretely assembled by means of the results of 401 independent CW single-frequency tests, each at a successively higher frequency.

Figure 2.2 is a schematic of the transmitter subsystem. In the actual system, the computer directs the HP-83623A to generate the specified frequency which is then amplified and sent to the transmission antenna. This same signal is also tapped to an RF-to-IF converter (HP-8511A) where the IF signal is then sent to the network analyzer (HP-8530A) for for signal detection. The magnitude and phase of the transmitted signal are

Figure 2.3: Simplified schematic of the receiver system and means for characterizing the received signal.

then extracted in a fashion following that depicted in Figure 2.4. This procedure is known as "quadrature" detection and can be thought of as a mixing operation that translates the received (tapped) signal to baseband to recover amplitude and phase in the form of quadrature components.

The in-phase component (or "I" component) is created by multiplying the transmitted signal by a reference signal generated by the mixer oscillator. The input signal is defined as:

$$B_1 \cos(2\pi f t + \phi_1) \qquad \qquad \text{Eq(2.2)}$$

The mixer reference signal, generated at the same frequency, but different amplitude and phase, is:

$$B_2 \cos(2\pi ft + \phi_2) \qquad \qquad \text{Eq(2.3)}$$

The result of multiplying the two signals is:

$$B_1B_2\cos(2\pi ft + \phi_1)\cos(2\pi ft + \phi_2)$$
 Eq(2.4)



Figure 2.4: Schematic representation of a down conversion "mixer" used for quadrature detection in both the transmitted and received signals. In the NIST NLS tests, a common mixer oscillator was used as the reference for both signals.

Eq (2.3) can be expanded by means of standard trigonometric identities to yield:

$$B_1 B_2 \begin{pmatrix} \frac{1}{2} \cos(\omega t + \phi_1 - (\omega t + \phi_2)) \\ + \\ \frac{1}{2} \cos(\omega t + \phi_1 + (\omega t + \phi_2)) \end{pmatrix} \quad \text{Eq (2.5)}$$

where term ω , the cyclic frequency, is used interchangeably with the term $2\pi f$. By collecting terms this can be re-written as Eq(2.6):

$$B_1 B_2 \left(\frac{1}{2} \cos(\phi_1 - \phi_2) + \frac{1}{2} \cos(2\omega t + \phi_1 + \phi_2) \right)$$

The first component in Eq(2.6) represents the DC signal or "bias" component and does not depend on frequency. It does, however, contain information relating to the phase difference between the input (transmitted) and reference signals.

In order to extract on the first part, the composite signal is typically run through a low pass filter. The output from the low pass filter, for the in-phase component is:

$$\frac{B_1 B_2}{2} \cos(\phi_1 - \phi_2) \equiv I$$
 Eq (2.7)

where the "I" is used to indicate that this term characterizes the real or "in-phase" component of the input signal. In a similar fashion the quadrature (or imaginary) component of the complex input signal can be generated by phase shifting the input signal by $\pi/2$ radians. The resulting "quadrature" signal is:

$$B_1 B_2 \left(\frac{1}{2} \sin(\phi_1 - \phi_2) + \frac{1}{2} \cos(2\omega t + \phi_1 + \phi_2) \right)$$

Eq(2.8)

Passing this signal through a low-pass filter yields the "quadrature" (or imaginary) component of the input signal as:

$$\frac{B_1 B_2}{2} \sin(\phi_1 - \phi_2) \equiv Q \qquad \qquad \text{Eq (2.9)}$$

The transmitted signal, at the discrete frequency, f_0 , can now be completely characterized as:

$$S_{T} = I_{T} + jQ_{T} \qquad Eq(2.10)$$

where

$$j = \sqrt{-1}$$

The transmit signal amplitude is:

$$A_T = \sqrt{{I_T}^2 + {Q_T}^2} \qquad \text{Eq (2.11)}$$

The same procedure (quadrature detection) is applied to the received signal, as depicted in Figure 2.3. In this situation there is an important additional consideration in that, although we are transmitting continuously at the selected discrete frequency, f_0 , there may (and and almost always will) be other components of the signal, at different frequencies and phases, resulting from multipath reflections, refraction and other dispersive phenomena. In order to eliminate these unwanted secondary signals, the receiver is tuned to listen at the specified frequency, f₀, by means of a narrow band pass filter. The band error typical of the NIST tests was \pm 20 KHz. In the particular implementation described in Figure 2.3, the same mixer reference signal is used for quadrature detection as that shown in Figure 2.2. The resulting received signalis given by:

$$S_{R} = I_{R} + jQ_{R} \qquad Eq(2.12)$$

At this point it will be useful to switch to phasor notation to describe the process by which the attenuation and phase angle are derived. Phasor notation is based on the equality:

$$e^{j\theta} = \cos\theta + j\sin\theta$$
 Eq (2.13)

Using this notation, the received signal is:

$$B = B\cos(2\pi f_0 + \phi_B)$$

= Real(Be^{j(2\pi f_0 + \phi_B)}) Eq (2.14)
= Real(Be^{j\phi_B}e^{j(2\pi f_0)})

and the transmitted signal is:

The ratio of the received to transmitted signals, as depicted in Figure 2.5, is:

$$\tilde{C}_{RAW} = \frac{\tilde{B}_{RECEIVE}}{\tilde{A}_{TRANSMIT}} \qquad \qquad \text{Eq (2.16)}$$

If we substitute Eqs(2.14 and 2.15) into Eq(2.16) we obtain:

$$\frac{\tilde{B}}{\tilde{A}} = \frac{Be^{j\phi_B}}{Ae^{j\phi_A}}$$
 Eq (2.17)
$$= \frac{B}{A}e^{j(\phi_B - \phi_A)}$$

The amplitude ratio, B/A, in the above equation represents the attenuation of the signal as a result of propagation through a dispersive medium. The ratio varies from 0.0 to 1.0 with 1.0 representing transmission in a vacuum (ideal transmission) and 0.0 representing complete attenuation (absorption and reflection) by the media. The phase angle difference in the exponent is a measure of the time of flight between the transmitter and receiver, including dispersion-related group velocity effects as the signal propagates through engineering materials.



Figure 2.5: Impulse synthesis approach used in the NIST NLS tests. Composite signals with bandwidths of 1.5 and 5 GHz, respectively, were achieved by recording the response for discrete single frequency transmissions. The composite time domain response was synthesized via chirp-Z transform from the discrete frequency response spectrum.

$$\frac{\tilde{B}}{\tilde{A}} = \frac{B\cos\phi_B + jB\sin\phi_B}{A\cos\phi_A + jA\sin\phi_A}$$

$$I_R = B\cos\phi_B$$

$$Q_R = jB\sin\phi_B$$

$$I_T = A\cos\phi_A$$

$$Q_A = jA\sin\phi_A$$
Eq (2.18)

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as expressed in Eqs(2.10) and (2.12) above. We can thus proceed directly to write that the ratio of received to transmitted signals is given by:

$$\frac{S_R}{S_T} = \frac{B}{\tilde{A}} = \frac{I_R + jQ_R}{I_T + jQ_T} \qquad \text{Eq (2.19)}$$

Eq(2.19) represents a complex division of the form [6]:

From Eq(2.18) it is apparent that the values of I_R , Q_R , IT, and QT can be determined via quadrature detection

$$\frac{A}{C} = \frac{a+jb}{c+jd}$$

$$= \frac{(ac+bd)+j(bc-ad)}{a^2+b^2}$$
Eq (2.20)
$$= \frac{(ac+bd)}{a^2+b^2} + \frac{j(bc-ad)}{a^2+b^2}$$

The solution for the ratio of the received to transmitted signals, at the discrete frequency, f_0 , being investigated as:

$$\tilde{C}_{RAW} = \frac{S_R}{S_T} = \frac{\tilde{B}}{\tilde{A}} =$$
 Eq (2.21)

$$\frac{(I_R I_T + Q_R Q_T)}{{I_R}^2 + {Q_R}^2} + j \frac{(Q_R I_T - I_R Q_T)}{{I_R}^2 + {Q_R}^2}$$

$$= I_{RAW} + jQ_{RAW}$$

As shown in Figure 2.5, this procedure is carried out for each discrete frequency of interest with the ultimate objective of building a discrete frequency response spectrum for a given bandwidth of interest. However, the results presented in Eq(2.21) represent uncalibrated, or "raw" data. There are a number of factors which need to be taken into account.

The most important of the corrections involves deviations in the signal propagation velocity through the atmosphere. As previously discussed, the objective is to determine the time of flight of the signal from the transmitting antenna to the receiving antenna. The conversion to distance involves the velocity of electromagnetic radiation in the atmosphere, as given by Eq(2.1). Small errors in the determination of the propagation velocity can lead to large errors in the straight line distance estimate. Empirical correction factors have been derived for propagation of radio waves through the atmosphere as follows:

Eq (2.22)

$$N = \frac{77.6p}{T} + \frac{373000e}{T^2}$$
$$n = 1 + \frac{N}{10^6}$$

$$C_{atmosphere} = \frac{C_{vacuum}}{n}$$

whereN=scaled-up refractivityp=total pressure in millibarse=partial pressure of water vapor
in millibarsT=absolute temperature in
degrees Kelvincvacuum=speed of light in a
vacuum

In addition there are also errors which result from the internal electrical nature of the radar instrument. For example, the length and efficiency of the coaxial cables which connect the antennas to the system and the efficiency with which signals are propagated through the various electrical subsystems.

Fortunately, there is an elegant, and simple method for accounting for all of these sources of error, both due to propagation through the atmospheric and from instrumental error, by means of a calibration procedure [5]. This involves the generation of a point for point discrete frequency response spectrum, using the same techniques outlined above, but with the important difference that the setup be a line of sight test over a known, precision surveyed bench. The bench consists of two benchmarks whose positions have been established relative to one another using standard total station surveying equipment. The resulting "freespace" response is used to calibrate the raw data by dividing the raw signal, at each discrete frequency, by the freespace result, as shown in Figure 2.5, following Equation(2.23):

$$\tilde{C}_{CALIBRATED} = \frac{\tilde{C}_{RAW}}{\tilde{C}_{FREESPACE}}$$

The freespace signal is defined as

$$S_F = \tilde{C}_{FREESPACE} = I_F + jQ_F \qquad \text{Eq (2.24)}$$

where the notation is the same as previously used to describe the normalized in-phase and quadrature components for the raw signal defined in Eq (2.21). The F subscripts in Eq(2.24) denote the freespace calibration. Equation 2.23 can now be rewritten as:

Eq (2.25)

$$\tilde{C}_{CALIBRATED} = \frac{C_{RAW}}{\tilde{C}_{FREESPACE}} =$$

$$\frac{I_{RAW} + jQ_{RAW}}{I_{FREESPACE} + jQ_{FREESPACE}} =$$

$$\frac{\left(I_{RAW}I_{FREE} + Q_{RAW}Q_{FREE}\right)}{I_{RAW}^{2} + Q_{RAW}^{2}} +$$

$$j \frac{\left(Q_{RAW}I_{FREE} - I_{RAW}Q_{FREE}\right)}{I_{RAW}^{2} + Q_{RAW}^{2}}$$

where

$$I_{RAW} = \left(\frac{(I_{R}I_{T} + Q_{R}Q_{T})}{{I_{R}}^{2} + {Q_{R}}^{2}}\right)_{RAW}$$

$$Q_{RAW} = \left(\frac{\left(Q_{R}I_{T} - I_{R}Q_{T}\right)}{I_{R}^{2} + Q_{R}^{2}}\right)_{RAW}$$

$$I_{FREE} = \left(\frac{\left(I_R I_T + Q_R Q_T\right)}{I_R^2 + Q_R^2}\right)_{FREE}$$

$$Q_{FREE} = \left(\frac{\left(Q_R I_T - I_R Q_T\right)}{I_R^2 + Q_R^2}\right)_{FREE}$$

For the NLS tests conducted at NIST, the above calculations were performed in a post-processing mode since the data acquisition system was only designed to write one file at a time. Thus, the freespace response was always acquired prior to the commencement of any day's testing. Furthermore, a second freespace measurement was made at the end of each day to compare against any changes that might have occurred during the day. Subsequent to the freespace measurement, raw experimental data files were created for each material test following Eq(2.21). The final calibration, following Eq(2.25), was performed as part of an automated MatLab post-processing script that operated on all data files.

The calibrated frequency response spectra were stored as a 5 x n matrix, where n was the number of discrete frequencies sampled. As previously described, 401 evenly spaced points were acquired for the 0.5 to.0 GHz tests and 801 points were acquired for the 3.0 to 8.0 GHz tests. For each frequency, the I and Q values (I_{CALIBRATED} and Q_{CALIBRATED} (Eq.2.25) were stored in the second and third columns respectively. The fourth column contained the derived calibrated, normalized amplitude, as given by Eq(2.11). Specifically, for the calibrated signal, the amplitude is calculated as:

$$A_{CALIBRATED} =$$

Eq (2.26)

$$\sqrt{\mathbf{I}_{\text{CALIBRATED}}^2 + Q_{CALIBRATED}^2}$$

This is a decimal value between 0.0 and 1.0, with 1.0 meaning that there was no attenuation observed during the test for which a material specimen was placed between the transmitter and receiver, relative to the same freespace test. The decimal amplitude may easily be converted to decibels (dB):

 $A(dB) = 20 * \log_{10} A(decimal)$

In addition, the phase angle (radians) for the calibrated response signal was stored in the fifth column in each calibrated data file. The phase angle is:

$$\phi_{CALIBRATED} = \tan^{-1} \left(\frac{Q_{CALIBRATED}}{I_{CALIBRATED}} \right) \quad Eq(2.28)$$

In the attenuation versus frequency plot presented later in the paper the frequency (in GHz) is plotted on the x-axis while the decimal version of Eq(2.26) is plotted on the y-axis. Efforts have been made to fit simplified closed form solutions to these curves for the purposes of characterizing the attenuation characteristics of a broad range of materials over a very wide frequency bandwidth while maintaining a manageable and compact means for accessing that data (see Table 7.1). Such equations are available, e.g., for all of the materials listed in Table 5.2 [3].

3: Antenna Descriptions

Two antenna geometries have been used for the NIST test program. The first, originally manufactured by Watkins-Johnson* and now fabricated by Condor Systems, had a bandwidth of 1.5 GHz between 0.5 and 2.0 GHz. The second, manufactured by Flam and Russell, had a bandwidth of 5 GHz from 3.0 to 8.0 GHz. Where polarization capability existed, the V-V polarization configuration was employed for the NIST tests, as initial studies [1] clearly indicated that multipath distortion due to ground bounce was minimized through the use of a vertically polarized plane wave transmission.

These antennas provide high-gain directional patterns over multi-octave bandwidths. Each pyramidal horn (Figure 3.1) has two orthogonally placed input feeds which provide the capability for simultaneous horizontal and vertical polarization. For the attenuation tests reported herein, only the vertical polarization was used. A typical implementation is shown in Figures 3.2 and 3.3, where attenuation and distance measurements are being taken for a composite specimen consisting of



Figure 3.1: Quadridged 0.5 to 2.0 GHz . Vertical polarization, used for NIST tests, used only the two central vertical ridges.

three back-to-back masonry block walls.

A relatively broad area of illumination is provided by this design. Although signal power is reduced by approximately one half (3dB) by an azimuth angle of 30 degrees to either side of center, considerable signal strength can still be measured at azimuth angles of 90degrees. Because of the relatively different radiation pattern geometry for this antenna, as contrasted with that for the 3.0 to 8.0 GHz diagonal horn described below, results pertaining to attenuation of transmitted power, tend to be antenna specific.

For tests in the range of 3.0 to 8.0 GHz FR6400 class range illumination horns from Flam & Russell,

Figure 3.2 (Right): Experimental calibration of a composite wall consisting of three back-to-back 76 mm brick walls. The wall sections measure 1 meter square. The 3 mm thick aluminum panel in background served as a multipath signal shield.





Figure 3.3: Isometric view of test stand for Phase 2 NLS tests. Mobile table is shown with specimen in place on opposite side of EM shield from transmitting horn.

Inc. were used. These horn antennas produce radiation patterns with low sidelobe structure, nearly circularly symmetric beam, and nominally constant gain and beamwidth.

The particular model used for the NLS tests was the FR-6415 3.0 to 8.0 GHz horn, which was designed to serve as a source antenna in the measurement of antenna radiation patterns or as transmit and receive antennas in the measurement of radar cross-section data. These antennas exhibit significantly reduced Eplane sidelobes typically associated with horn antennas. The FR-6415 incorporates aperture defocusing to produce minimal variations in gain and beamwidth over a frequency range of 2.5:1.

Figure 3.4 shows a typical laboratory setup involving the FR-6415 in which the effect of a 203 mm thick reinforced concrete wall on time-of-flight distance measurement is being conducted. A frequency response spectrum was generated from 3.0 to 8.0 GHz with this system.

4: Test Fixtures

Because of the large number of test specimens, and the representative full-size thicknesses used for the various materials, a test set-up was designed that made use of an indoor laboratory at NIST equipped with an overhead crane. The set-up is shown in isometric view in Figures 3.3 and 3.4.

Previous tests with the radar system [1] had shown the problematic nature of multipath signals reaching, and distorting, the straight line (through the specimen) transmission signal. Calculations showed that an electromagnetic shield, in the form of a roughly 2.5 m square, 3 mm thick aluminum panel would effectively separate any multipath signals from the data except for those due to internal reflections within the specimen thickness. This was accurate provided the transmitting and receiving horns were relatively close to the test article. The distance selected was 1 m from the backplane of the EM shield to the aperture of each antenna. This meant that the distance from the receiving horn to the back side of the specimen varied, depending on the specimen thickness.

The EM shield contained a 914 mm square "window" on centerline through which the transmitted signals could pass unobstructed, as shown in Figures 3.3 and 3.4. Multipath signals diffracting around the edges of the shield arrived significantly later (in the time domain) and were thus easily eliminated using gating windows.



Figure 3.4: Oblique photo of the indoor NLS test range at NIST. The transmitting antenna is on the left. The receiving antenna (at right) was positioned behind an aluminum shield to insure that the data were not corrupted by multipath signals. The entire center section moved laterally, so that effects of material variance (inhomogeneity) could be investigated.

In order to gain statistical data concerning the variability of the measured distance with respect to the spatial and compositional variability of the various materials, the entire specimen carrier platform was mounted to a rail system that permitted translation of the specimen perpendicular to the line of signal transmission. In this manner, several duplicate sets of tests could be conducted for a single specimen, but with different sections of the specimen being located on the centerline of the transmission path.

5: Specimen Design

A total of 9 different materials were tested in this series. A summary of these is presented in Table 5.1. More detailed statistics are given in [3]. The test articles included common construction materials such as brick, masonry block, plain concrete, reinforced concrete, glass, lumber, plywood, drywall, and reinforcing rods. At least three different thicknesses, and in some cases four, were tested for each of the above materials. In addition, the lumber and plywood specimens were tested in both a wet and dry state.

Of particular interest is the list of plain concrete specimens in Table 5.1. Because of the widely varying nature of this common composite, efforts were made to construct an experiment matrix that captured some of the most important variables. These included aggregate size, water/cement ratio, and slump. The full material design matrix included high and low values for each of the above three parameters plus three panel thicknesses for a total of 24 plain concrete specimens. Reinforced concrete and reinforcing rod grids (in air) were investigated separately in order to quantify the affects of the reinforcing.

All specimens had a 1 m by 1 m cross section. Design thicknesses varied from as little as 6 mm to as much as 600 mm depending on the material and typical usage values at commercial and residential construction sites. Complete details on specimen geometry, material properties, as well as calibrated attenuation data from 0.5 through 8 GHz are given in [3].

6: Test Protocol

The data for each test consisted of a calibrated frequency response spectrum. The theory and hardware instrumentation which allows for the generation of this spectra were presented in Section 2. These techniques were implemented in an automatic fashion via computer control.

All SDecin	nens to be 1m	x 1m square						
* Receiver 1	Unit to be el	ectromagnet	ically isolate	d from muli	tipath by mea	ans		
of an alun	ninum plate	shield (3mm	thick sheet,	extending 1r	n minimum			
about a ce	ntral 95 cm x	95 cm squar	e hole					
* Transmis	sion and rece	eiver antenna	is located 1m	from oppos	ite sides of			
the pane.	ls (2.0 m spac	ing between	antennas)					
* All tests a	are conducte	d using both	frequency b	andwidths a	available: 0.50	00-		
2.0 Ghz (set 1); 3-8 Gh	z (set 2).						
* For concr	ete specimer	is the follow	ing propertie	es apply:				
Properties	Batch 1	Batch 2	Batch 3	Batch 4	Batch 5	Batch 6	Batch 7	Batch 8
MSA	0.5	0.5	0.5	0.5	1	1	1	1
w/c	0.0	0.0	0.6	0.6	0.4	0.4	0.6	0.6
Slump	low	high	10147	high	low	high	10147	high
% Comont	15.9	18.2	10.5	12.1	14.1	160	9.4	10.7
% Water	10.0	22.9	10.0	22.9	17.8	20.2	17.8	20.2
% CA	20.0	22.9	20.0	22.9	37.0	20.2	27.0	20.2
0/ EA	29.9	29.9	27.5	22.5	28.6	24.3	37.5	20.7
% Pacto	25.7	41.1	37.2	35.0	20.0	24.5	27.2	20.0
70 Faste	btc SSD Baci	41.1	per cubic m	eter (kg/m	A3)	30.2	27.2	30.9
Comont	407 C	5, Kilograms	221 7	291 7	445.2	504 7	204 7	226
Wator	497.0	278.9	100.2	228.0	177.9	202.1	177.8	202
water	199.2	220.9	912.2	220.9	1/7.0	1022.1	1022.1	1022
EA	015.5	615.5	072.9	852.7	750.2	637.2	972.0	1052.
FA	035.9	095.0 95.0	973.0	033.7	750.3	037.3	0/3.9	07
Density	00.9	85.5	05.0	04.4	09.1	00.0	00.2	07.
Course Mgg	regute. no i	in in (Duice),	ir nor (buter				
For each ba For the Rer	th there will naining Eng	be 3 thicknes ineering Ma	ss: 102 mm, 2 terials the fo	203 mm, and ollowing cha	305 mm racteristics a	pply:		
For each ba For the Rer Mat	th there will naining Eng erial	be 3 thicknes ineering Ma Thickness	ss: 102 mm, 2 terials the fo Thickness	203 mm, and ollowing cha Thickness	305 mm racteristics a Thickness	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A	th there will naining Eng erial rrete Concrete	be 3 thickness ineering Ma Thickness 203.2	ss: 102 mm, 2 terials the fo Thickness N/A	203 mm, and ollowing cha Thickness N/A	305 mm racteristics a Thickness N/A	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2 Type A	th there will naining Eng erial rete Concrete Grade 60 rete Concrete	be 3 thickness ineering Ma Thickness 203.2	ss: 102 mm, 2 terials the fo Thickness N/A	203 mm, and ollowing cha Thickness N/A	305 mm racteristics a Thickness N/A	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2, Type A 2% Mesh, G	th there will naining Eng erial rete Concrete Grade 60 rete Concrete Grade 60	be 3 thickness ineering Ma Thickness 203.2 203.2	ss: 102 mm, 2 terials the fo Thickness N/A N/A	203 mm, and ollowing cha Thickness N/A N/A	305 mm racteristics a Thickness N/A N/A	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2, Type A 2% Mesh, G Glass(Plair	th there will naining Eng erial rete Concrete Grade 60 rete Concrete Grade 60 1)	be 3 thickness ineering Ma Thickness 203.2 203.2 6.4	ss: 102 mm, 2 terials the fo Thickness N/A N/A 12.7	203 mm, and billowing cha Thickness N/A N/A 19.1	305 mm racteristics a Thickness N/A N/A	pply:		
For each ba For the Ren Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2, Type A 2% Mesh, G Glass(Plair Drywall	th there will naining Eng erial rrete Concrete Grade 60 rrete Concrete Grade 60 1)	be 3 thickness ineering Ma Thickness 203.2 203.2 6.4 6.4	ss: 102 mm, 2 terials the fo Thickness N/A N/A 12.7 9.5	203 mm, and bilowing cha Thickness N/A N/A 19.1 12.7	305 mm racteristics a Thickness N/A N/A	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2, Type A 2% Mesh, G Glass(Plair Drywall Plywood	th there will naining Eng erial rrete Concrete Grade 60 rrete Concrete Grade 60 1)	be 3 thickness ineering Ma 203.2 203.2 203.2 6.4 6.4 6.4 203.2	ss: 102 mm, 2 terials the fo Thickness N/A N/A 12.7 9.5 12.7 406 4	203 mm, and billowing cha Thickness N/A N/A 19.1 12.7 19.1 19.1	305 mm racteristics a Thickness N/A N/A N/A 31.8	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2, Type A 2% Mesh, G Glass(Plair Drywall Plywood Masonry Bl	th there will naining Eng erial crete Grade 60 crete Grade 60 concrete Grade 60 concrete Grade 60	be 3 thickness ineering Ma 203.2 203.2 203.2 6.4 6.4 6.4 6.4 203.2 203.2	ss: 102 mm, 2 terials the fo Thickness N/A N/A 12.7 9.5 12.7 9.5 12.7 406.4 76 2	203 mm, and bilowing cha Thickness N/A N/A 19.1 12.7 19.1 609.6 114.2	305 mm racteristics a Thickness N/A N/A 31.8	pply:		
For each ba For the Rer Mat Reinf. Conc # 1, Type A 1% Mesh, G Reinf. Conc # 2, Type A 2% Mesh, G Glass(Plair Drywall Plywood Masonry Bl Southern Pi	th there will naining Eng erial crete Concrete Grade 60 rete Concrete Grade 60 h) ock	be 3 thickness ineering Ma Thickness 203.2 203.2 203.2 6.4 6.4 6.4 6.4 203.2 38.1 203.2	ss: 102 mm, 2 terials the fo Thickness N/A N/A 12.7 9.5 12.7 406.4 76.2 177.0	203 mm, and bllowing cha Thickness N/A N/A 19.1 12.7 19.1 609.6 114.3 2467	305 mm racteristics a Thickness N/A N/A 31.8 152.4	pply:		

The protocol for testing any specimen, however, consisted of the following steps:

Step 1: Acquire freespace response spectra. At the start and finish of each day of testing a response spectrum was acquired using the test setup configured as shown in Figure 3.4, but with no specimen loaded. This was later used in the calibration of the raw signal as previously discussed. Step 2: Acquire response spectrum for the test specimen. This step follows the previously described theoretical protocol for discrete construction of the response spectrum but with one important variation. Instead of a single measurement being made at each frequency, an average of 128 samples of the response at each frequency was recorded. This was performed automatically and was done to increase the accuracy of each individual frequency response measurement. The same procedure was used for the freespace measurements.





Step 3: Spatial variation tests. Ten separate tests were performed for each physical specimen. After each test the specimen platform was moved in 6 mm increments perpendicular to the signal transmission line between the two horns and the test repeated until a maximum displacement of 60 mm had been achieved. Each individual test was calibrated during the post processing cycle as described in Section 2.1. Using these ten separate tests, mean and standard deviation of the frequency response spectra for a particular specimen could be determined. It was this averaged frequency response spectrum that was used for subsequent time domain analyses.

7: Post-Processing Procedures

Several post-processing techniques were used to improve the utility of the attenuation spectra. First, the averaged frequency spectra for a given test specimen was converted to time domain using a chirp-Z transform [7]. The implementation used for the tests reported here was an embedded function in DATAPRO (a proprietary code developed by Flam & Russell) which was part of the experimental instrumentation. This transform can also be achieved using stand-alone post-processors such as, Matlab [8] and other digital signal processing packages. The chirp-Z transform was used because it is



Figure 7.2: Calibrated time domain response for 152 mm thick brick wall (no post processing) for the 0.5 to 2.0 GHz test series, Specimen #1 of 10.

much faster than an FFT when prime length sequences are involved. In the case of the data presented here, there were 401 discretely sampled points which composed the 0.5 to 2.0 GHz data and 801 points which composed the 3.0 to 8.0 GHz data. A typical input file would be a frequency response spectrum like that shown in Figure 7.1 for the 0.5 to 2.0 GHz test series. In this case, the data shown are for a 152 mm thick, double "wythe" brick wall, that is, a brick wall two blocks deep, similar to that shown in Figure 3.3. Using a chirpz transform, the data in Figure 7.1 can be converted to the time domain plot shown in Figure 7.2. This is a particularly good data set, with very little attenuation involved. In fact, as can be seen for certain frequencies around 0.75 GHz in Figure 7.1, the calibrated frequency response is actually slightly greater than 1.0, implying that constructive "ringing" or "beating" is taking place within the wall. This will not normally be the case, especially with thicker, denser walls such as concrete.

The time domain plot shown in Figure 7.2 shows one predominant peak at a range of slightly more than two meters. Two observations need to be made at this point. First, a "time domain" data set implies amplitude as a function of time, usually expressed in seconds. In this case, the scale is actually in nanoseconds, where 1



Figure 7.3: Gated time domain response for 152 mm thick brick wall for the 0.5 to 2.0 GHz test series, Specimen #1 of 10.

nanosecond of electromagnetic wave travel in free space is equivalent to approximately 305 mm (or 1 ft). This equivalence permits a recasting of the x-axis scale in the more useful units of distance. The second point is that the true distance between the two antennas was pre-set at 2.000 meters. The peak in Figure 7.2 clearly is not at 2.000 meters. The difference, approximately 205 mm, is almost entirely due to group-velocity lag time as the signal propagates through the target. During its transit through the brick wall, the signal travels (relative to our reference frame) at a velocity much smaller than the speed of light in a vacuum. For many engineering materials, for example reinforced concrete, the propagation velocity through the material can be as much as nine times less than the speed of light in a vacuum. This is important for the development of compensation algorithms to account for these errors in surveying instruments.

Adjacent to the predominant peak in Figure 7.2 are several ripples or side lobes. In general these will be much more pronounced in materials with higher water content and the signal to noise ratio is lower. It should also be noted that even for this case there is a substantial amount of noise in the frequency response spectra shown in Figure 7.1. This noise in the frequency spectrum is produced by both ringing (internal reflections within the target) and multipath signals. Since the true distance was known with high accuracy for these experiments, a range gate [9]on the time domain can be used to clean up the frequency response spectra.

The HP 8530A used for these experiments contains a gating feature which allows for selective viewing of individual portions of the time domain response. The "gate" is actually a band-pass shaped time domain filter. The user has direct control over the gate width and location including the selection of the gate start and stop times and the gate center. For the NIST data, the gate center was assigned to the maximum amplitude peak in the time domain response. The specific gating used was a 1 nanosecond wide Kaiser-Bessel window centered on the peak, which effectively considered only those data within a 6 dB amplitude variation from the peak. The result of the application of this gate in the time domain is shown in Figure 7.3 for the case of the brick wall previously considered.

An inverse transform of the time domain data yields the gated frequency response spectra (see Figure 7.4). This is a much cleaner representation of the attenuation characteristics of the transmitted signal with respect to frequency. The actual processing of the data proceeded in a step-wise fashion as follows:

- Define the time gates to use for each material sample using DATAPRO.
- Apply the time gating to each measurement with DATAPRO, and save the gated frequency and time domain data in Network Common Data Form (netCDF).
- Read the netCDF data and perform statistical analysis on the gated frequency and time domain data using MatLab.
- Write out the averages and standard deviations of the measurements for each sample in both netCDF and ASCII files.

The data presented in Figure 7.4 are typical of those obtained for all but the thickest concrete specimens tested. These data show, beyond doubt, that extremely small baseband transmission power levels (1 milliwatt was the level used in these experiments) are sufficient to penetrate nearly all common construction materials, other than solid metal. Reinforced concrete walls as thick as 500 mm have been successfully penetrated during the course of the NIST tests. For common residential construction, involving 2x4 frames, drywall, and either plywood, masonry block or brick exteriors, the materials are nearly "transparent," as far as NLS is





concerned, with only minimal power attenuation. Further, because propagation delay times are directly proportional to material density, these latter materials produce smaller deviations from the true distance. It therefore seems likely that NLS technology will first be used for registered-view component placement in residential construction. Its use for precision machine control and component tracking and placement in more cluttered environments will require the use of real-time propagation compensation techniques. These procedures, which include both hardware and software, are being developed at NIST under the aegis of the construction automation and robotics program at the Building and Fire Research Laboratory.

8: Conclusions

This research project addressed the subject of automated metrology (surveying) for use on construction sites. Specifically, the experimental program has been directed towards the practical development of a novel Non-Line-of-Sight (NLS) survey system with which the real-time position and orientation (attitude) of any object on a construction job site may be determined, irrespective of the presence of intervening obstacles that would otherwise render optical, electro-optical, and other short wavelength electromagnetic distancing techniques useless.

Tests were conducted using a specially configured broadband low frequency spread spectrum radar operating between 0.5 to 8.0 GHz. The transmission and receiving antennae, which in normal radar are typical-

Table 7.1: Regression Coefficients (DECIMAL) for BRICK Transmission versus Frequency Curves Plotted in Figure 4.1a. The regression equation is of the form

Transmission Coefficient = M0+M1*F+M2*F^2+M3*F^3+M4*F^4+M5*F^5+M6*F^6, where F is the frequency in GHz. The standard error term, R, is defined in the text.

Brick Attenuation Cu	irves								
		Regression Coefficients							
Curve Identification	Format	MO	M1	M2	M3	M4	M5	M6	R
D11	Decimal	3 9639	-14.581	28.08	-29.294	17.034	-5.1913	0.64614	0.99991
B1L + sigma	Decimal	4.5257	-17.17	32.792	-33.64	19.218	-5.7648	0.70796	0.99994
B11 - sigma	Decimal	3.402	-11.993	23.368	-24.947	14.849	-4.6177	0.58433	0.99986
821	Decimal	1.0632	-1.5358	2.6528	-3.1728	2.1941	-0.77778	0.10904	0.99999
B2L + sigma	Decimal	1.518	-3.8092	7.087	-7.5039	4.4849	-1.4097	0.18071	0.99998
B2L - sigma	Decimal	0.60845	0. 73763	-1.7813	1.1583	-0.096713	-0.14587	0.037369	0.99999
	Desimal	1 2602	-2 6303	4 8103	-5.7441	3,9546	-1.4052	0.1983	0.99998
B3L + sigma	Decimal	1.722	-4.9095	9.2863	-10.126	6.2539	-2.0278	0.26699	0.99998
B3L - sigma	Decimal	0.81643	-0.35111	0.33429	-1.362	1.6553	-0.78258	0.12961	0.99998

Data are for the Frequency Range 0.5 to 2.0 GHz.

ly one and the same, were physically separated so as to create a system with a fixed broadcast unit and a "roving" receiver, whose range was to be determined relative to the transmission antenna by means of time-ofarrival measurements.

Time domain response was synthesized by means of chirp-z Fourier theory from a broad spectrum of data sampled in the frequency domain. Numerous field and laboratory experiments were performed in which typical construction site obstacles were placed between the transmitter and receiver with separation distances of up to 70 meters in the case of the outdoor tests. The outdoor obstacles included a half-meter thick, heavily reinforced concrete wall, varying combinations of masonry block and brick up to two meters in thickness and at varying angle-of-incidence orientations relative to the transmission path, and metal pre-fabricated wall panels. In all but the latter case, repeatable distance measurements were obtained.

Range detection was lost in the presence of extensive metal panels which contained no windows. However, the presence of even small openings (on the order of several centimeters) permitted range acquisition. Subsequent, extensive, laboratory measurements quantified the behavior of 58 different construction materials involving 1160 tests over two frequency bandwidths (0.5 to 2.0 GHz and 3.0 to 8.0 GHz). In all cases, unambiguous distance measurements could be acquired. Error sources in the laboratory tests were largely defined by the delay times involved with the propagation of electromagnetic radiation through the These errors were highly construction materials. repeatable, suggesting an avenue towards the development of auto-compensation techniques.

Several types of problems well known to the radar community were observed during the outdoor tests. These included "clutter" (reflections of the transmitted beam off false "targets") and "multipath" (diffracted and scattered elements of the original signal which may, under certain conditions, arrive ahead of the desired signal and which, as a matter of course, may obscure or cast doubt upon which detected signal in the time domain response represents the true transmitter-to-target distance).

The other phenomena, described earlier, is the well known fact that electromagnetic radiation propagates through solid media at velocities less than the speed of light in a vacuum. Thus, any signal transmitted through an engineering material -- e.g. brick, masonry block, or concrete walls -- will appear to have been delayed from its expected arrival time at the receiver. In some cases this delay was sufficient that multipath signals arrived ahead of the "true" signal representing the straight line distance from transmitter to receiver. The delay is directly proportional to the dielectric and the permittivity constants of the engineering material penetrated. Where long distances are involved between the transmitter and receiver the characteristics of the air (including temperature, humidity, and barometric pressure) must be accounted for as well. During the NIST tests this was accomplished automatically by means of a "free space" calibration with no intervening obstacles between the transmitter and receiver at the start of each test series.

Errors due to propagation delays can be significant. Penetration of a half-meter thick outdoor reinforced concrete wall induced a mean range error of 800 mm. For combined masonry block walls faced with brick, range errors of three meters were observed for a wall thickness of *two* meters and a half meter error for a wall thickness of 300 mm. Subsequent extensive laboratory tests showed these range errors to be linearly proportional to the penetration depth (wall thickness) and to the dielectric constant for the material.

While three meters of range error over a 70 m survey shot is unacceptable for modern construction surveying, it is important to recognize that nearly all of the error is related to propagation delay. The more surprising result is that a measurement through two meters of brick and masonry block was achieved at all! Open field tests [10] have since demonstrated that 10 mm accuracy or better is achievable using this system. This suggests that it is feasible to develop real-time compensation techniques which will be capable of eliminating errors due to propagation. The development of such a method is currently being investigated at NIST.

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